

Show work where possible rate = k rate = $k[A]^2$ $[A]_t = -kt + [A]_0$ $\ln[A]_t = -kt + \ln[A]_0$ $\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$

$$t_{1/2} = 0.693/k \quad t_{1/2} = 1/(k[A]_0) \quad \ln \frac{k_2}{k_1} = \frac{E_a}{R} \left(\frac{1}{T_1} - \frac{1}{T_2} \right) \quad R = 8.314 \text{ J/mol}\cdot\text{K}$$

1. The reaction $\text{H}_2(\text{g}) + \text{I}_2(\text{g}) \rightarrow 2\text{HI}(\text{g})$ was found to have the following rate constant values:

@556 K, $k = 1.2 \times 10^{-4} \text{ M}^{-1}\text{s}^{-1}$ and @666 K, $k = 3.8 \times 10^{-2} \text{ M}^{-1}\text{s}^{-1}$.

a. (6 Pts) Determine the activation energy.

$$\ln \frac{1.2 \times 10^{-4}}{3.8 \times 10^{-2}} = \frac{E_a}{8.314 \frac{\text{J}}{\text{mol}\cdot\text{K}}} \left(\frac{1}{666} - \frac{1}{556} \right)$$

$$E_a = 160000 \frac{\text{J}}{\text{mol}} \quad \text{or} \quad 1.6 \times 10^5 \text{ J/mol}$$

161 kJ/mol

b. (6 Pts) At what temperature will the rate constant have a value of $1.0 \times 10^{-3} \text{ M}^{-1}\text{s}^{-1}$?

$$\ln \frac{1.0 \times 10^{-3}}{1.2 \times 10^{-4}} = \frac{1.6 \times 10^5}{8.314} \left(\frac{1}{556} - \frac{1}{T_2} \right)$$

$$T_2 = 592 \text{ K}$$

2a. (3 Pts) Determine the rate constant for a first order reaction with a half-life of 15.5 days.

$$t_{1/2} = \frac{\ln 2}{k} \quad k = \frac{\ln 2}{t_{1/2}} = \frac{0.693}{15.5 \text{ days}} = 0.0447 \text{ days}^{-1}$$

b. (4 Pts) How long will it take for the concentration the reactant in problem 2a to reach 90% of its starting concentration?

$$\ln [A]_t = -kt + \ln [A]_0$$

$$\ln [0.90] = -0.0447 \text{ days}^{-1} t + \ln [1]$$

$$t = 2.36 \text{ days}$$

3. (6 Pts) A reaction that is second order in one reactant has a rate constant of $1.0 \times 10^{-2} \text{ L mol}^{-1} \text{ s}^{-1}$ at 25 °C. If the initial concentration of the reactant is 0.100 M, how long will it take for the concentration to become 0.0500 M?

$$\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$$

$$\frac{1}{0.0500} = 1.0 \times 10^{-2} \text{ M}^{-1} \text{ s}^{-1} (t) + \frac{1}{0.100}$$

$$t = 1000 \text{ seconds}$$